

# PM 346 Assignment 2 - Due Jan 30.

1. Describe all homomorphisms from  $C_6$  to  $S_3$
2. Describe all homomorphisms from  $S_3$  to  $C_6$
3. Describe all automorphisms of  $(\mathbb{Q}, +)$
4. If  $H$  and  $N$  are subgroups of  $G$  we define the product  $H \cdot N = \{hn : h \in H, n \in N\}$ 
  - a) Prove that if  $N$  is normal in  $G$ , then  $HN$  is a subgroup of  $G$
  - b) Prove that if  $H$  and  $N$  are both normal in  $G$ , then  $HN$  is a normal subgroup of  $G$
  - c) Prove that  $H \cap N$  is a subgroup of  $G$
  - d) Prove that if  $N$  is a normal subgroup of  $G$ , then  $H \cap N$  is a normal subgroup of  $H$ .
5. Prove that if  $H$  and  $N$  are normal subgroups of  $G$  and  $H \cap N = \{1\}$ , then  $\forall a \in H$  and  $\forall b \in N$  we have  $ab = ba$ .